

PHYS 1403 Stars and Galaxies



Recap of Important Laws

1. What is Galileo's law of falling body?
In the absence of friction the acceleration due to gravity is constant.
For Earth g is 9.8 m/s^2

Recap of Important Laws

1. What are Newton's Laws of Motion?
Law of Inertia:
A body stays at rest or in uniform motion until and unless an external force acts on it.
Law of Force:
Acceleration of a body is proportional to the force it experiences and inversely proportional to the mass it has.
Law of Action and Reaction:
For every action there is equal and opposite reaction.

Recap of Important Laws

1. What are Kepler's laws of planetary motion?
Law of Ellipses:
A planet revolves around the Sun in an ellipse, a circle is a special type of ellipse.
Law of Equal Areas:
A planet moves faster when it is closer to the Sun and slower when it is farthest from the Sun.
Law of Periods:
The period squared is equal to the cube of semi-major axis of the ellipse.

Questions for Today's Class

1. Why do we need to study circular motion?
2. What is Centripetal force?
3. What is Newton's law of gravitation?
4. How do we describe Orbital Motion using Newton's Laws.

Why do we need to study circular motion?

Natural motion is not always straight line, many objects exhibit circular motion and stars and galaxies are no exception.

To describe motion of rotating bodies we use the terminology
Angular analogue for linear motion are

Topics

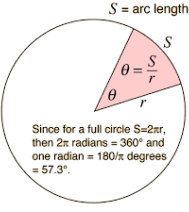
Radian
Angular speed
Angular Velocity
Angular Acceleration
Torque
Angular Momentum.

Radian

Radian: An angle at the center of a circle whose arc is equal in length to the radius

Units of Measure: Radian, Degrees and Revolutions

1 radian = 57.3 degrees



Source: wikipedia


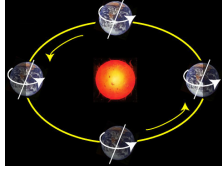
Angular Speed and Velocity

Angular speed (ω): How fast something is rotating

Angular Velocity (ω): How fast something is rotating, clockwise or counter clockwise

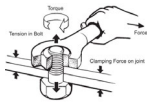
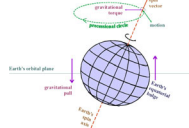
$\omega = \text{change in angle} / \text{change in time}$
SI units rad/s or rev/s, or deg/s

Angular Acceleration (α): How fast angular velocity is changing
 $\alpha = \text{change in } \omega / \text{change in time}$
SI units rad/s² or rev/s², or deg/s²

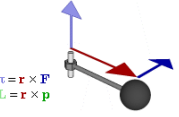
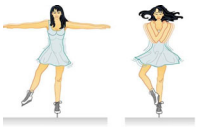
Torque and Angular Momentum

Torque (τ): How much force it takes to rotate something

Physics Stack Exchange UNLV Physics

Angular Momentum (L): How much momentum does a rotating body possess.

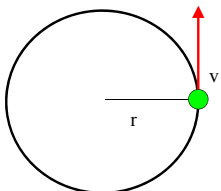
https://en.wikipedia.org/wiki/Angular_momentum

What is Centripetal Force?

1. Centripetal and Centrifugal Force
2. Visual Demo
3. Consequences of Centripetal Force in Astronomy

What is Centripetal Force?

- Any object that moves in a circle or an arc has centripetal force
- Centripetal force (F_c) measured in Newton's
 $F_c = ma = m v^2 / r$
- Centripetal (radial) acceleration
 $a_c = v^2 / r$



Circumference = $2 \pi r$
 $v = 2 \pi r / t$

Visual Demo of Centripetal Force

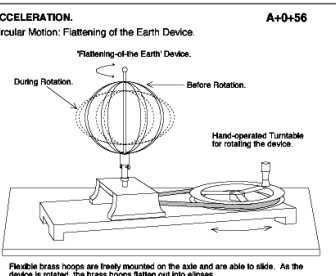
ACCELERATION: A+0+56

Circular Motion: Flattening of the Earth Device

"Flattening-of-the-Earth" Device

During Rotation. Before Rotation.

Hand-operated Turntable for rotating the device.

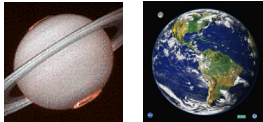


Flexible brass hoops are freely mounted on the axle and are able to slide. As the device is rotated, the brass hoops flatten out into ellipses.

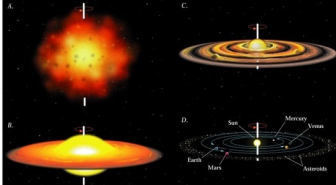

<https://www.youtube.com/watch?v=Tctr8CIMOZA>

Image source: NASA, STSI

Consequences of Centripetal Force



Why planets are not perfect spheres?

Solar System

Source: Wikipedia

Galaxy

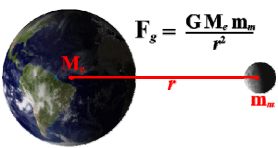
What is Newton's Law of Gravity?

1. Newton's Law of Gravity
2. Inverse Square Law
3. Gravitational Constant
4. Important Consequence of Newton's Laws

What is Newton's Law of Gravitation?

Any two bodies are attracting each other through gravitation, with a force (F_g) proportional to the product of their masses (M, m) and inversely proportional to the square of their distance (r). G is called gravitational constant.

$$F_g = \frac{GMm}{r^2}$$



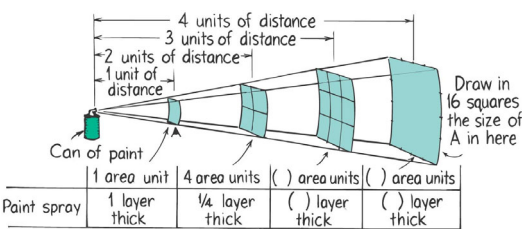
$$F_g = \frac{GM_e m_m}{r^2}$$

Gravity and Distance: The Inverse-Square Law

Inverse-square law -- $\frac{1}{r^2}$

- relates the intensity of an effect to the inverse-square of the distance from the cause
- in equation form: $intensity = 1/distance^2$
- for increases in distance, there is decreases in force
- even at great distances, force approaches but never reaches zero

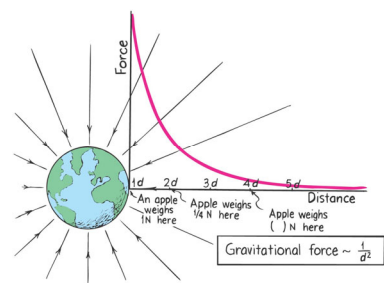
Inverse-Square Law



	1 unit of distance	2 units of distance	3 units of distance	4 units of distance
Paint spray	1 layer thick	1/4 layer thick	() layer thick	() layer thick
	1 area unit	4 area units	() area units	() area units

Can of paint, Draw in 16 squares the size of A in here

Force of Gravity and Inverse-Square Law



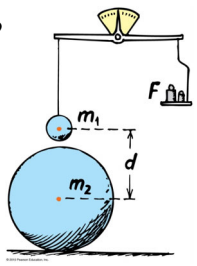
Gravitational force $\sim \frac{1}{d^2}$

Gravitational Constant

How to find the value of G?

$G = 6.67 \times 10^{-11} \text{ N.m}^2/\text{kg}^2$

$$F_g = \frac{Gm_1m_2}{d^2}$$



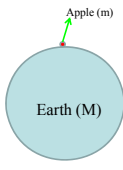
Gravitational force is significant only for very large masses and small separation distance

How to find the mass of Earth?

Weight = Gravitational Force

$$mg = \frac{GMm}{r^2}$$

$$M = \frac{g r^2}{G}$$

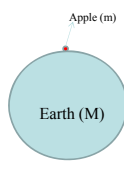


Since g, r and G are known we can calculate the mass of Earth = $6 \times 10^{24} \text{ kg}$

Acceleration due to Gravity g depends on Mass and Size of a Planet

Weight = Gravitational Force

$$mg = \frac{GMm}{r^2}$$

$$g = \frac{GM}{r^2}$$


If we know G, M and r then we can find g


Important Consequence of Newtons Laws

- Why Earth has to Move around Sun?
 - $a_{\text{sun}} = F/M_{\text{sun}}$
 - $a_{\text{earth}} = F / M_{\text{earth}}$
 - M_{sun} is 300,000 times larger than M_{earth}
 - Therefore a_{sun} is much smaller than a_{earth}
- The sun also moves slowly just as you would move if you swing a child in a circle.
- The center of mass is inside the Sun, therefore we see only a wobble motion.

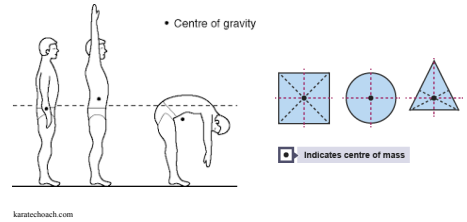
How do we describe orbital motion using Newton's Laws?

1. Center of mass and Gravity
2. Center of mass in Sun-Earth system
3. Types of Orbits
4. Geosynchronous Orbits
5. Escape Velocity
6. Artificial Gravity
7. Gravity Assist

Center of Gravity and Mass



Balance point of any System



• Centre of gravity

▣ Indicates centre of mass

Sun – Earth System

Earth- Sun System

Two Stars of Equal Mass

Star 1 is More Massive Than Star 2

Sun is Much More Massive Than Planet

Wikipedia.com

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<https://www.youtube.com/watch?v=1ISR3Yw6FXo>

Types of Orbits

Figure 4.1

What is the Velocity of Escape?

Rocket and Space Technology

Types of Orbits

(a) (b)

openstax

Escape Velocity

Escape velocity is the velocity required to escape the gravitational force of attraction of an astronomical body

$$v = \sqrt{\frac{2GM}{r}}$$

M = mass of the central body in kg
 G = gravitational constant (6.67×10⁻¹¹ m³/s²/kg)
 r = radius of the central body
 For Earth it is 11.2 km/s or 24,600 miles/hour

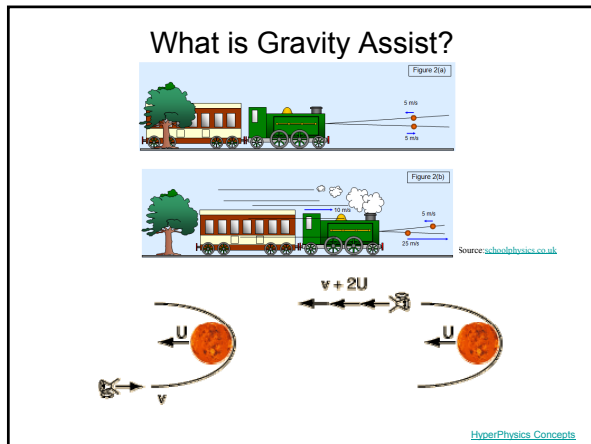
Can We Create Artificial Gravity?

ev.nrao.edu

Yes, But Technology is Challenging

<https://www.youtube.com/watch?v=3kqrV1.69mmA>

Image source: NASA, STSI



Wednesday class this week

- Complete Class Assignment 4



Acknowledgment

- The slides in this lecture is for Tarleton: PHYS1411/PHYS1403 class use only
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