

## § 8.4 Test of Hypothesis about a population Mean: z-stat

We really already covered this. To summarize:

$\mu_0$  - the status quo

$$z_c = \frac{\bar{x} - \mu_0}{\sigma_{\bar{x}}} = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}} \approx \frac{\bar{x} - \mu_0}{s/\sqrt{n}} \quad \text{- the test statistic generated by the sample}$$

$\alpha$  - significance level, Probability of a Type I error.

~~$z_c$  - critical value for the test. One-tailed:  $z_c = z_{\alpha}$~~   
 two-tailed:  $z_c = z_{\alpha/2}$ .

$P$  - observed significance level, generated by the sample.

	<u>One-tailed Tests</u>		<u>two-tailed</u>
	$H_0: \mu = \mu_0$	$H_0: \mu = \mu_0$	$H_0: \mu = \mu_0$
	$H_a: \mu < \mu_0$	$H_a: \mu > \mu_0$	$H_a: \mu \neq \mu_0$
rejection region	$z_c < -z_{\alpha}$	$z_c > z_{\alpha}$	$ z_c  > z_{\alpha/2}$
P-value	$P(z < z_c)$	$P(z > z_c)$	$2P(z >  z_c )$
reject $H_0$ :	$P < \alpha$ or $z_c$ in rejection region.		

Possible conclusions from the Test:

- (1) Reject  $H_0$ . The data supports  $H_a$ . State you are rejecting  $H_0$  at the  $\alpha$  level of significance.
- (2) Fail to reject  $H_0$  at the  $\alpha$  level of significance. The data does not support rejecting  $H_0$ .

Example Suppose  $\sigma = 60$  and a sample of 100 observations yields  $\bar{x} = 110$ . Test  $H_0: \mu = 100$ ,  $H_a: \mu > 100$  with  $\alpha = .05$ .

$Z_{\alpha} = 1.645$ , stat  $\rightarrow$  Tests  $\rightarrow$  z-test yields

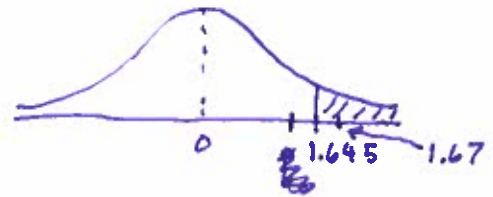
$$\mu > 100$$

$$Z_c = 1.67$$

$$P = 0.0478$$

$$\bar{x} = 110$$

$$n = 100$$



$Z_c > Z_{\alpha}$  and  $p < \alpha$  so

Reject  $H_0$  at the .05 significance level (observed significance level was 0.0478). The data supports  $H_a$ .

Example Suppose  $\sigma = 60$  and a sample of 100 observations yields  $\bar{x} = 110$ . Test  $H_0: \mu = 100$ ,  $H_a: \mu \neq 100$  with  $\alpha = .05$ .

$Z_{\alpha/2} = 1.96$ , stat  $\rightarrow$  tests  $\rightarrow$  z-test yields

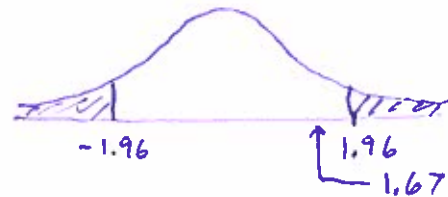
$$\mu \neq 100$$

$$Z_c = 1.67$$

$$P = 0.0956$$

$$\bar{x} = 110$$

$$n = 100$$



$|Z_c| < Z_{\alpha/2}$  ( $Z_c$  is not in rejection region) and  $p > \alpha$ .

Fail to reject  $H_0$  at a .05 significance level, the data does not support rejecting  $H_0$ .